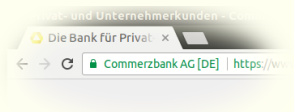


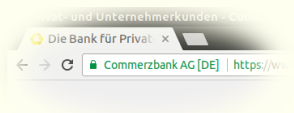
# On Assumptions and the Limits of Cryptography

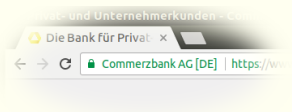
Nils Fleischhacker

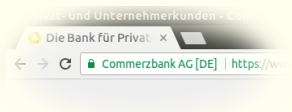
Bochum, January 23, 2019











So, how do we know all of this is secure?



## Heartbleed makes 50m Android phones vulnerable, data shows

Devices running Android 4.1.1 could be exploited by 'reverse Heartbleed' to yield user data - including 4m in US alone

## SSL BEAST Exposes Security Risk

BIZ & IT --

Critical crypto bug exposes Yahoo Mail, other passwords Russian roulette-style

OpenSSL defect still exposing sensitive data even after patch is released.

BIZ & IT --

"Lucky Thirteen" attack snarfs cookies protected by SSL encryption

Exploit is the latest to subvert crypto used to secure Web transactions.

### Security

The perfect CRIME? New HTTPS web hijack attack explained

BIZ & IT --

Gone in 30 seconds: New attack plucks secrets from HTTPS-protected pages

Exploit called BREACH bypasses the SSL crypto scheme protecting millions of sites.

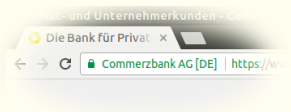
Vulnerability in SSL 3.0 Could Allow Information Disclosure

Alert! 20.05.2015 18:17 Uhr | Security

Logjam-Attacke: Verschlüsselung von zehntausenden Servern gefährdet

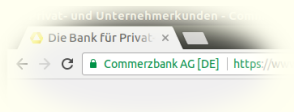
'Serious weaknesses' found in security protocol for web banking, Facebook

Cloudflare has been leaking private Uber, Fitbit and Ok Cupid details for months



Can we know whether all of this is secure?



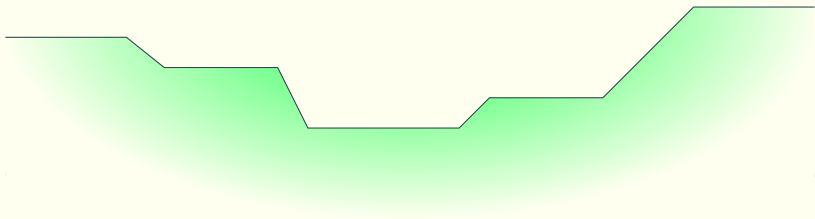


The sad truth is: At the moment **we can't!** Not really.

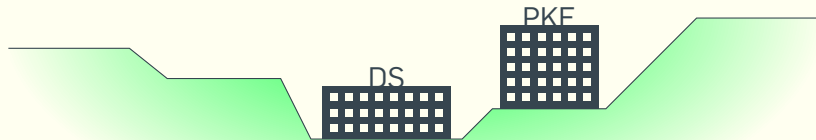




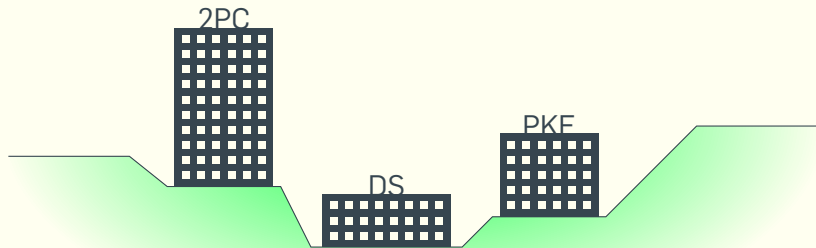
# The Cryptographic Landscape



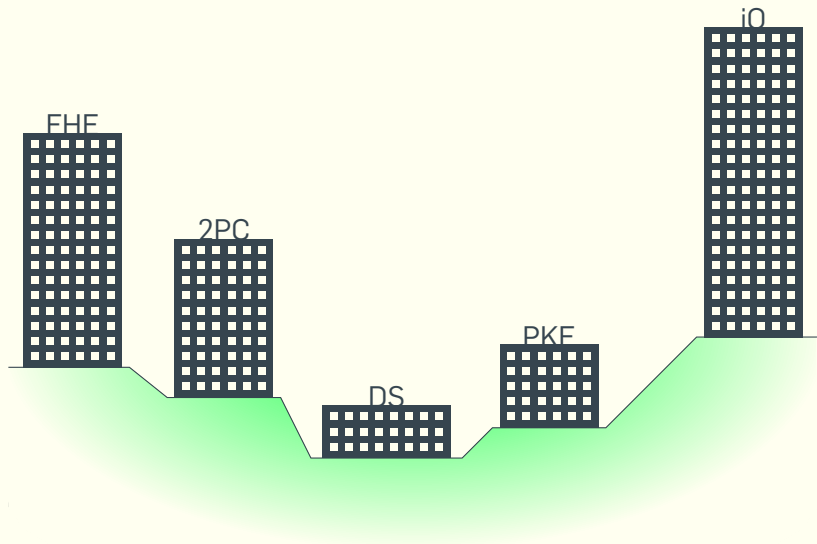
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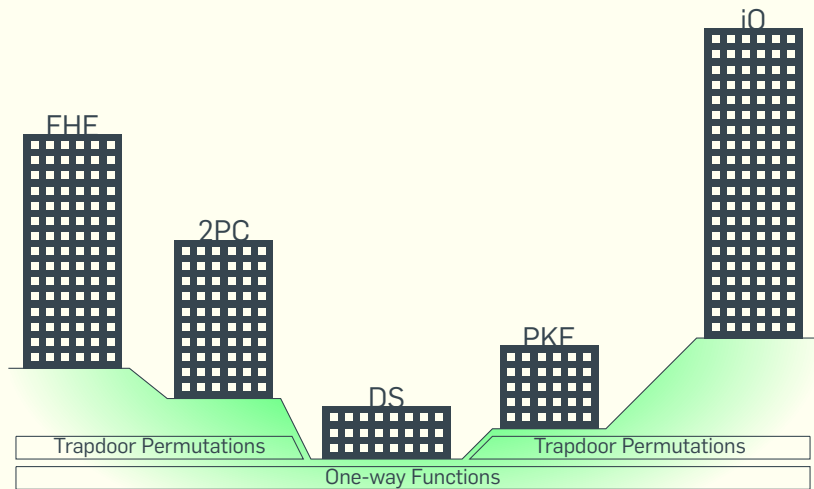
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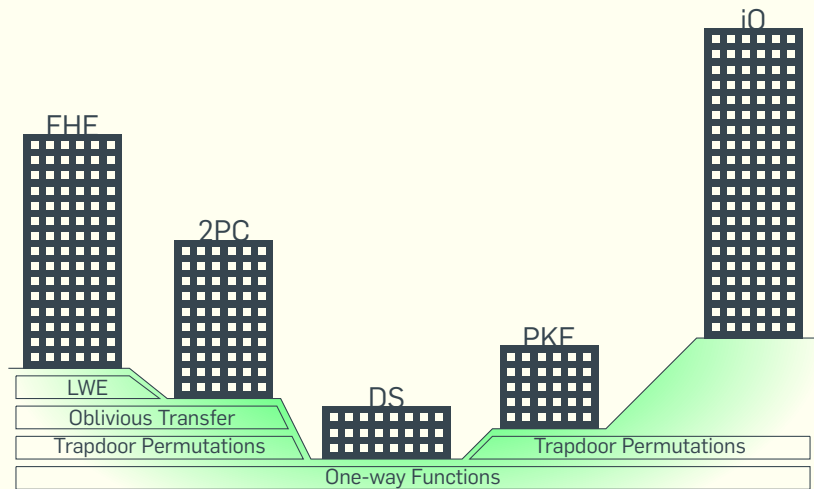
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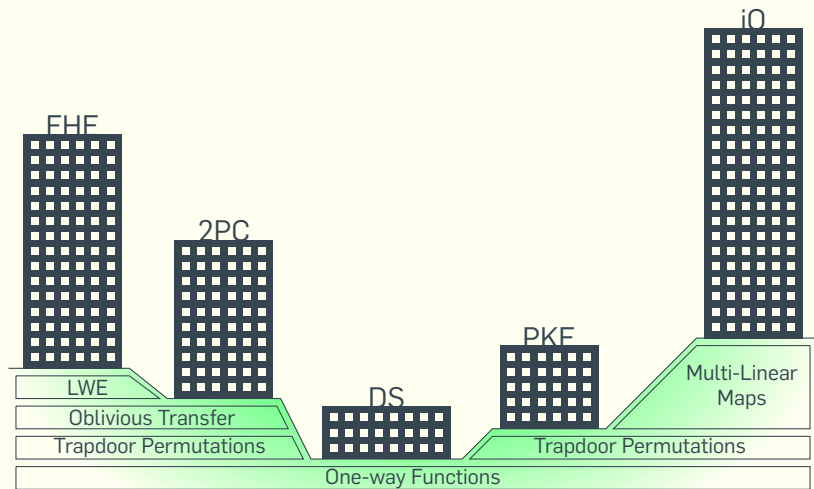
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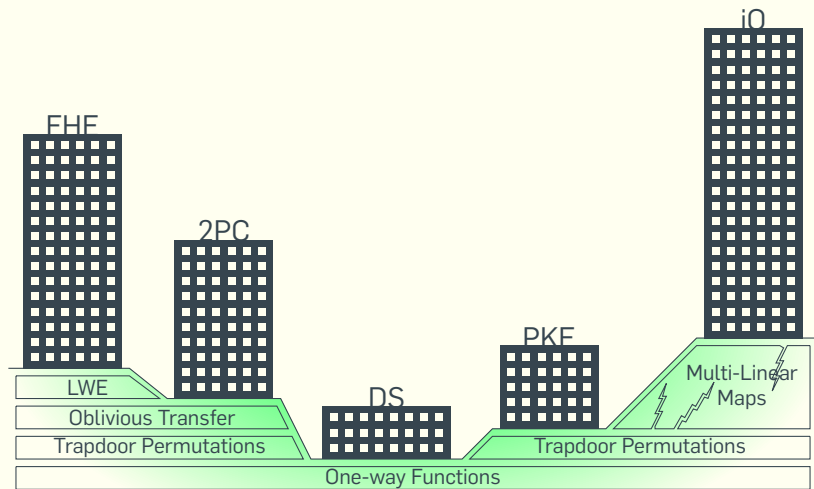
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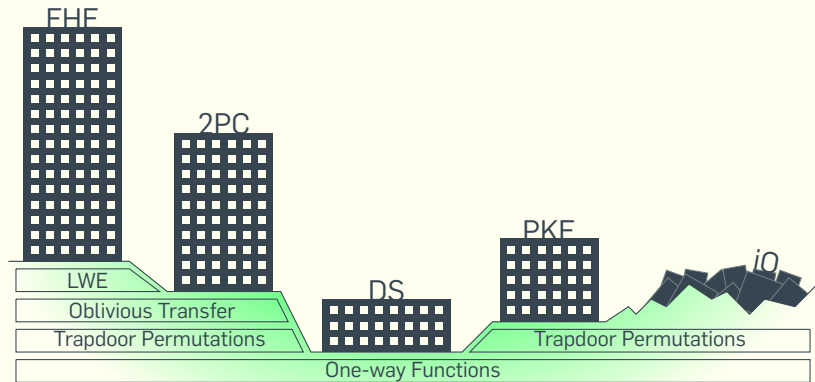


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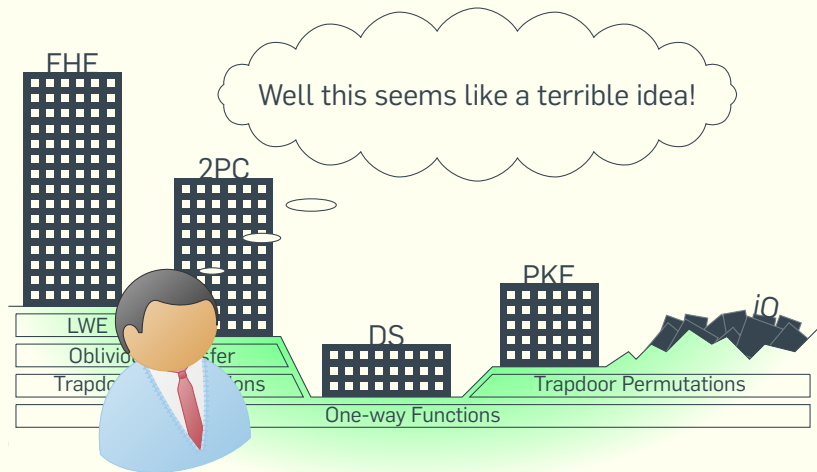




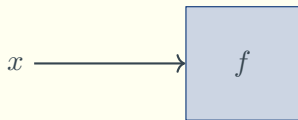
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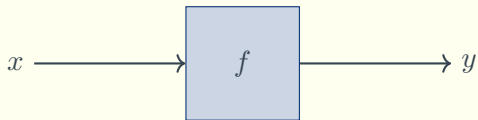
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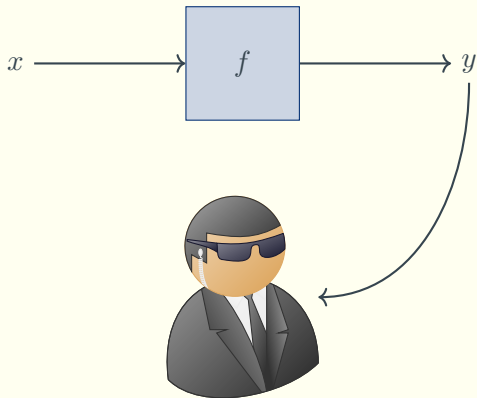
# One-Way Functions



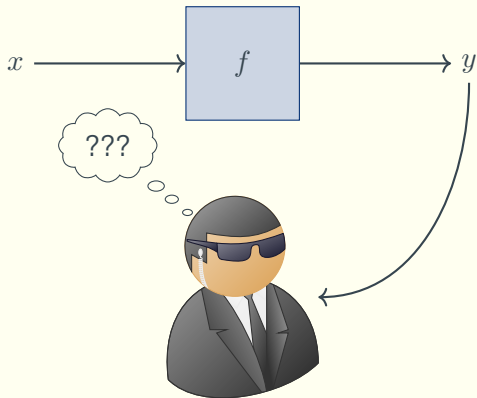
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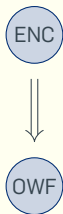


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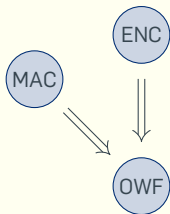
# Why We Need to Make Assumptions

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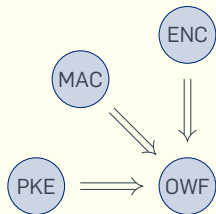




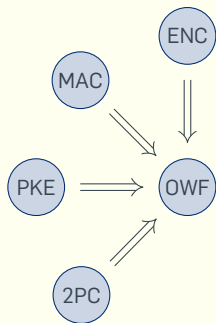
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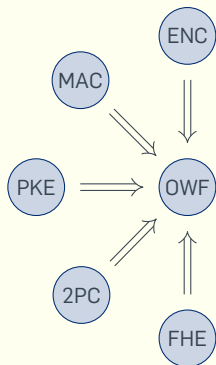
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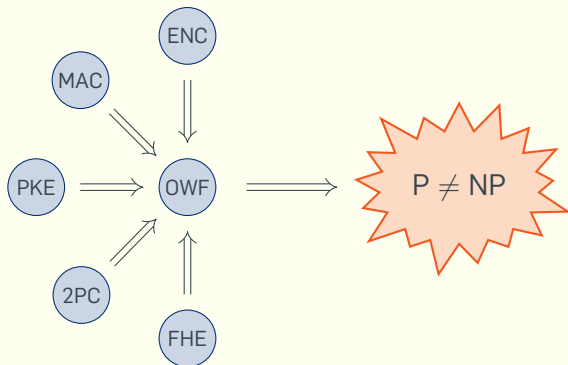
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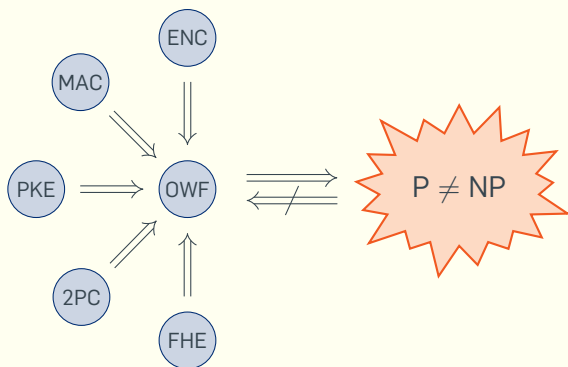
# Why We Need to Make Assumptions



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# Idea Behind Provable Security

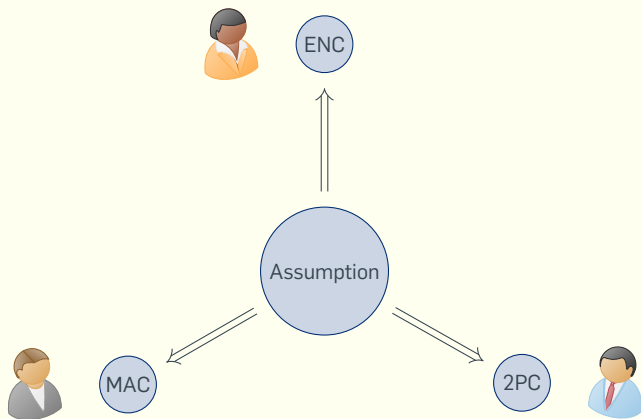


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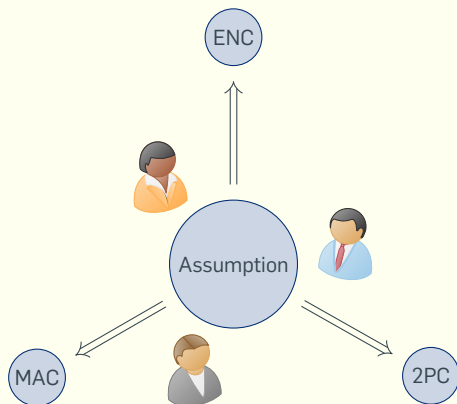




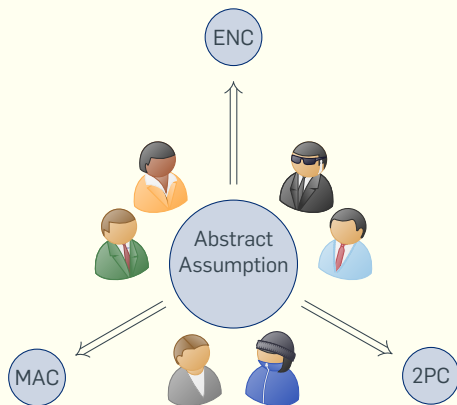
# Idea Behind Provable Security



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# Idea Behind Provable Security



## Determining Minimal Assumptions

Statistical Security

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One-Way Functions

Statistical Security

## Determining Minimal Assumptions

Trapdoor Permutations

One-Way Functions

Statistical Security

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Oblivious Transfer

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Statistical Security

## Determining Minimal Assumptions

⋮

Fully Homomorphic Encryption

⋮

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Statistical Security



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⋮

Fully Homomorphic Encryption

⋮

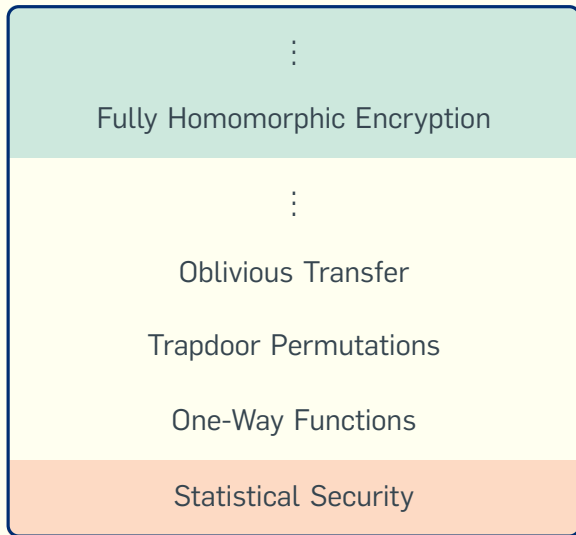
Oblivious Transfer

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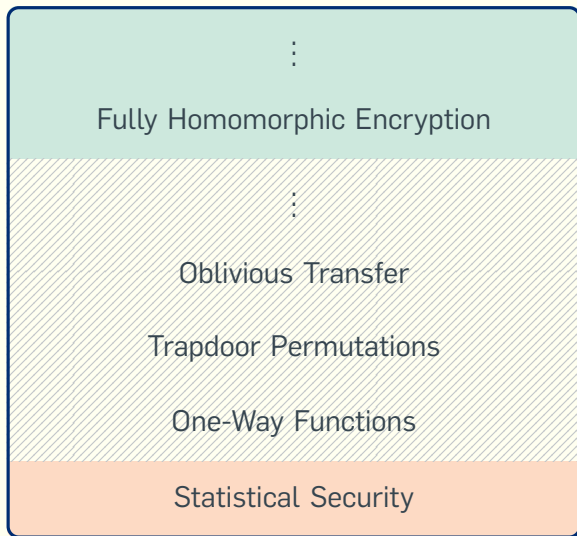
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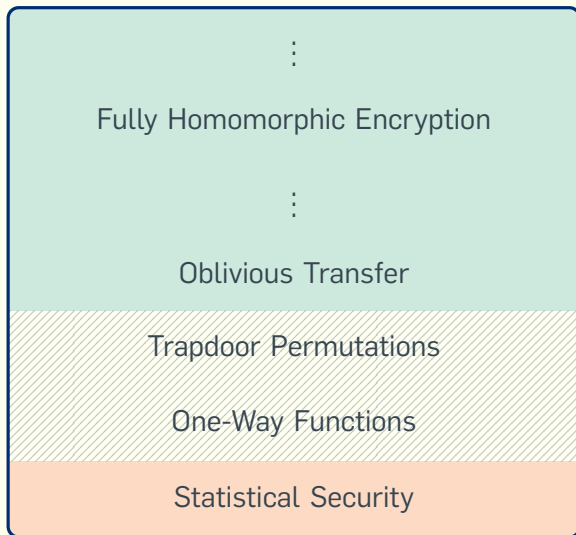
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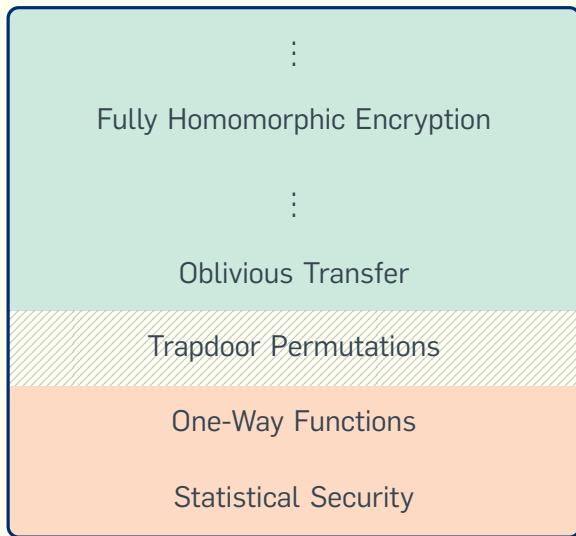
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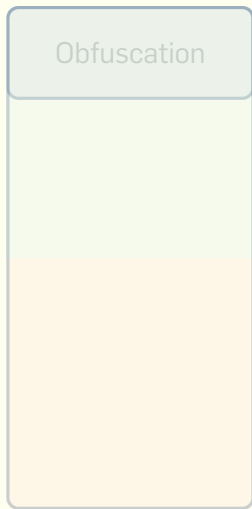
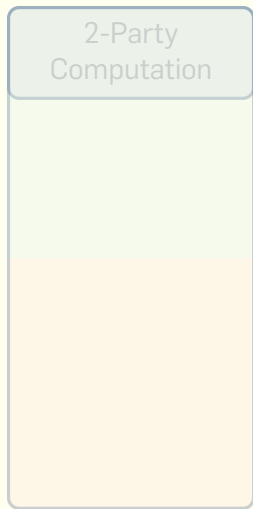
3-Round  
ZK-Proofs

2-Party  
Computation

Obfuscation



[FGJ18]



# Zero-Knowledge Proof Protocols

- ▶ A Zero-Knowledge Proof allows me to to prove that a statement is true without revealing the reason why.



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- ▶ A Zero-Knowledge Proof allows me to to prove that a statement is true without revealing the reason why.
- ▶ A ZK-Proof must be
  - ▶ Sound

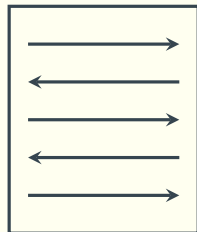
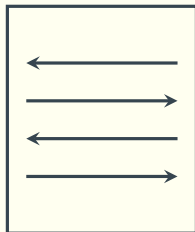
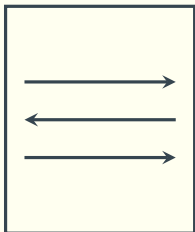
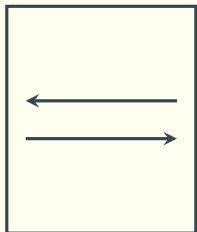
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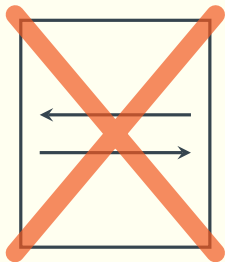
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- ▶ A Zero-Knowledge Proof allows me to to prove that a statement is true without revealing the reason why.
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- ▶ Incredibly useful tools in Cryptography

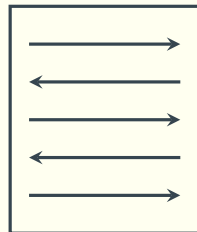
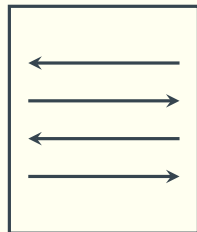
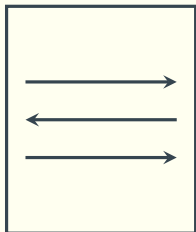
## Round-Complexity of ZK-Proofs for NP



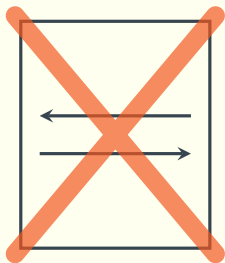
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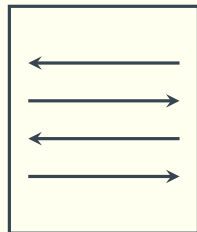
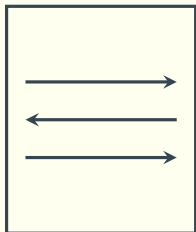
[G094]



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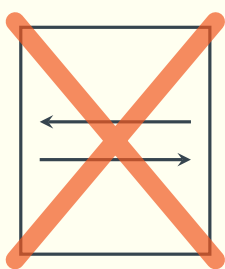


[G094]

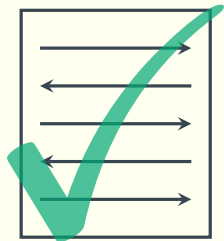
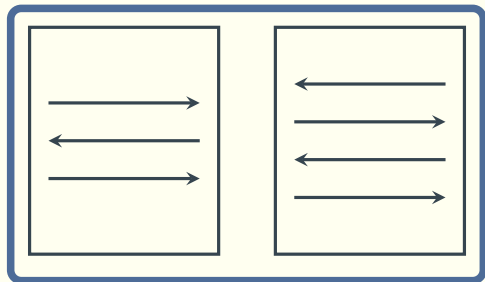


[GK96]

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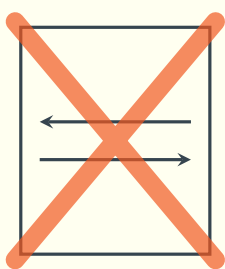


[G094]

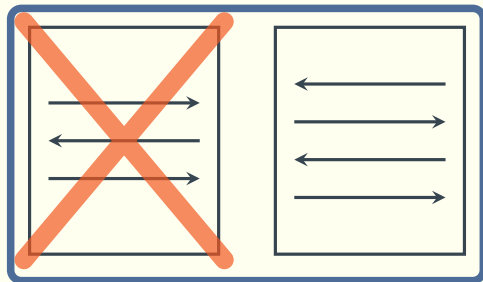


[GK96]

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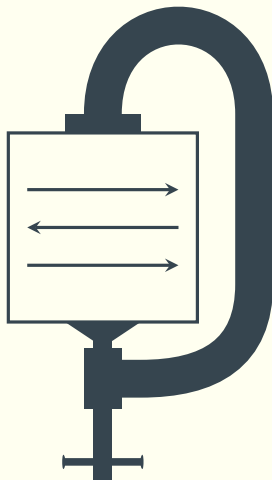
[G094]



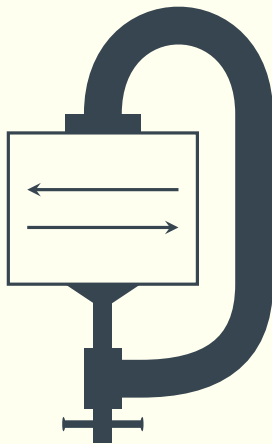
[GK96]



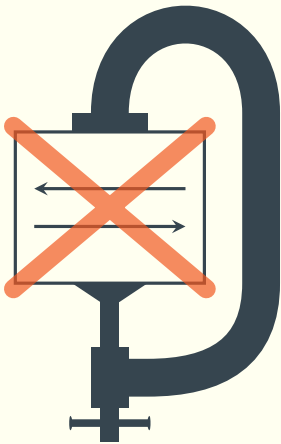
## Compressing Proofs



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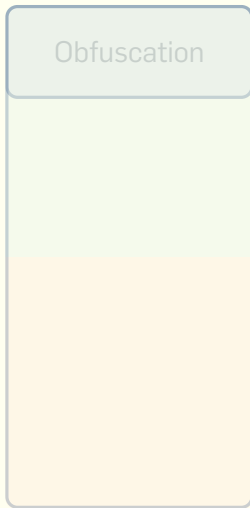




[FGJ18]



[DFKLS14]



## Secure Two-Party Computation from PUFs

- ▶ The idea: Use secure hardware to overcome impossibility of information theoretically secure 2-PC.

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- ▶ The idea: Use secure hardware to overcome impossibility of information theoretically secure 2-PC.
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# Secure Two-Party Computation from PUFs

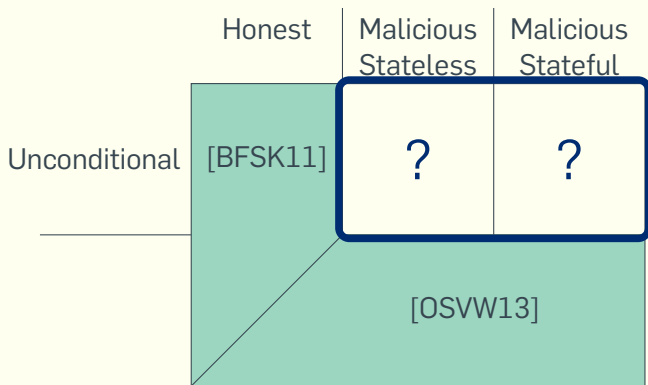
- ▶ The idea: Use secure hardware to overcome impossibility of information theoretically secure 2-PC.
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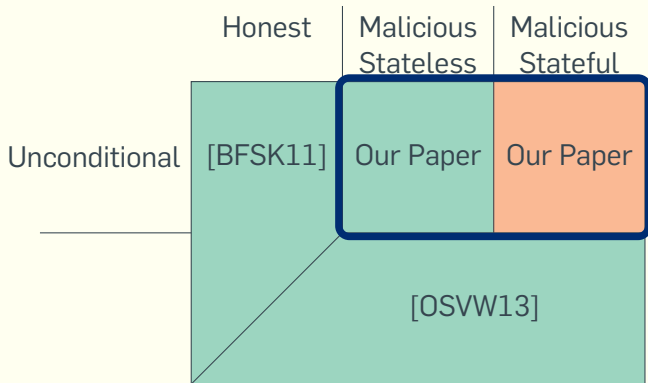
- ▶ The idea: Use secure hardware to overcome impossibility of information theoretically secure 2-PC.
- ▶ Use Physically Uncloneable Functions
  - ▶ Behave like random functions.
  - ▶ Cannot be copied.

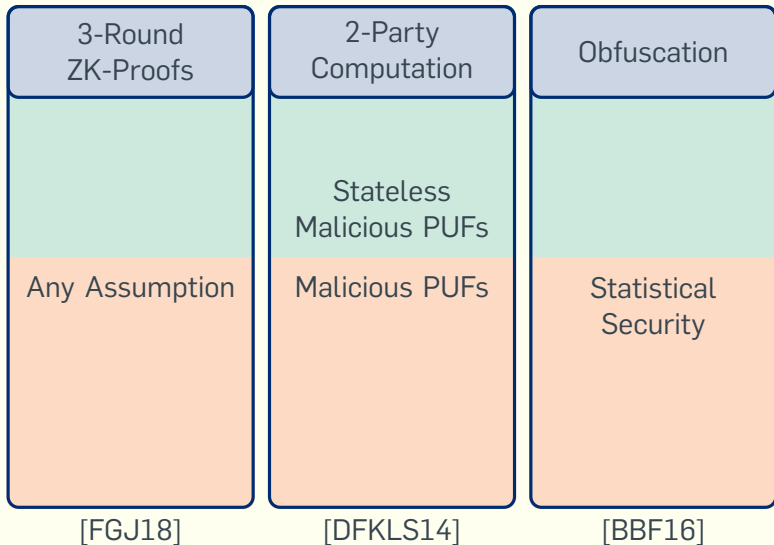


# Secure Computation from PUFs

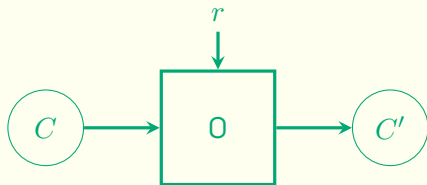


# Secure Computation from PUFs

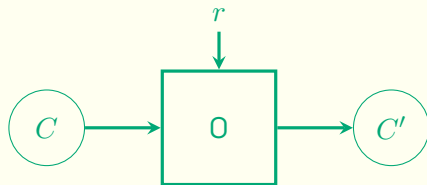




## Statistically Secure Obfuscation



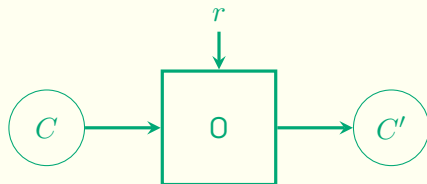
## Statistically Secure Obfuscation



- ▶ **Perfect Correctness:** For any circuit  $C$

$$\forall x : C'(x) = C(x)$$

## Statistically Secure Obfuscation



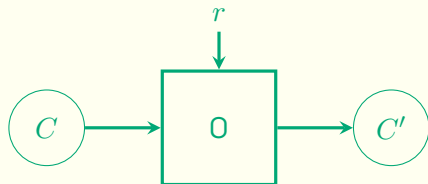
- ▶ ~~Perfect Correctness: For any circuit  $C$~~

$$\forall x : C'(x) = C(x)$$

- ▶  $(1 - \epsilon)$ -Approximate Correctness: For any circuit  $C$ ,

$$\Pr_{r,x} [C'(x) = C(x)] \geq 1 - \epsilon(n)$$

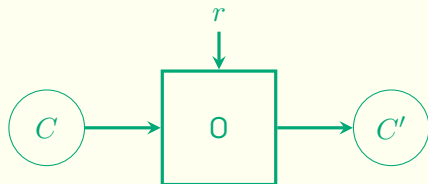
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- ▶ **Indistinguishability Obfuscator:** For any pair of circuits, such that  $C_1 \equiv C_2$  and  $|C_1| = |C_2|$

$$\text{SD}(O(C_1), O(C_2)) \leq \text{negl}(n)$$

# Statistically Secure Obfuscation



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- ▶  **$(1 - \delta)$ -Correlation Obfuscator:** For any pair of circuits, such that  $C_1 \equiv C_2$  and  $|C_1| = |C_2|$

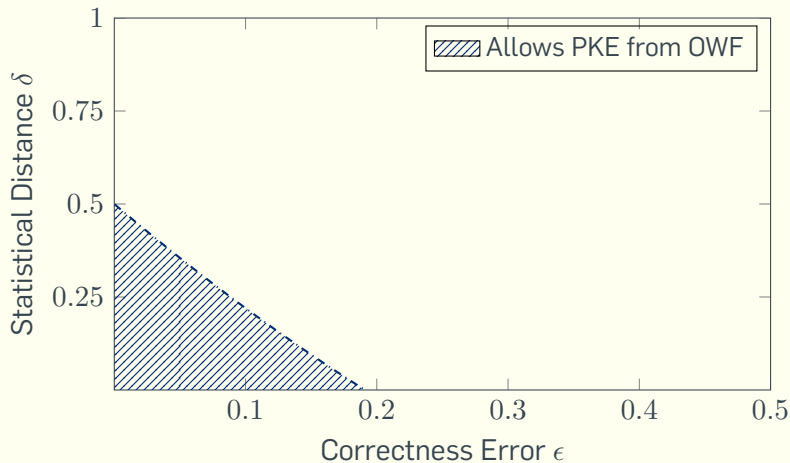
$$\text{SD}(O(C_1), O(C_2)) \leq \delta(n)$$



# Why Do We Even Care About Approximate Correctness?

Because approximate obfuscation is useful!

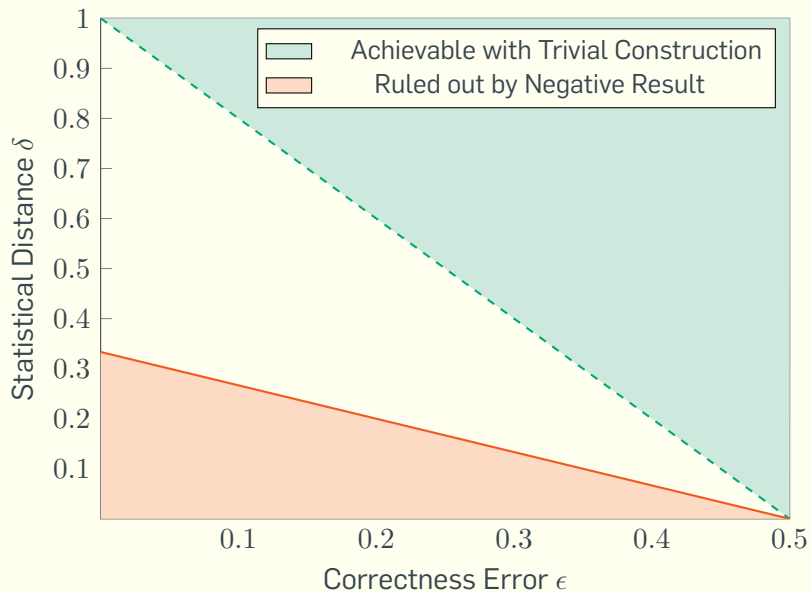
[MMNPs16,SW14,Hol06]



## Main Result

- ▶ If statistically secure, approximately correct iO (saiO) exists, then either one-way functions do not exist, or  $NP \subseteq AM \cap coAM$ .
- ▶ **More Generally:** If  $(1 - \delta)$ -statistically secure,  $(1 - \epsilon)$ -approximately correct correlation obfuscation (sacO) exists with  $\delta(n) \leq \frac{1}{3} - \frac{2}{3}\epsilon(n) - \frac{1}{\text{poly}(n)}$ , then either one-way functions do not exist, or  $NP \subseteq AM \cap coAM$ .
- ▶ For very weak parameters, a trivial construction of sacO exists with  $\delta(n) = 2\epsilon(n)$ .

# The Landscape of Correlation Obfuscation



# The Landscape of Correlation Obfuscation

